

# Addition

Year 3

- Add numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds.
- Add numbers with up to three digits, using formal written methods of columnar addition.
- Add fractions with the same denominator within 1 whole.
- Calculate the time taken by particular events or tasks.

Progression of skills

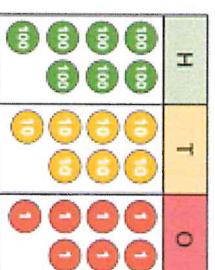
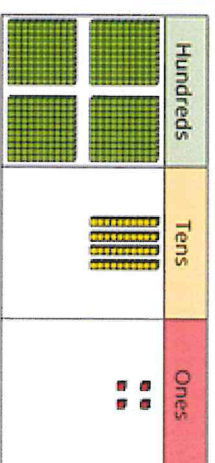
Key representations

Add 1s, 10s or 100s to a 3-digit number

Emphasis on mental strategies including number bonds and related facts. Prompt children to notice which digit changes.

The ones/tens/hundreds column will increase by ...

What patterns do you notice?



$$444 + 5 =$$

$$444 + 50 =$$

$$444 + 500 =$$

$$777 + 2 =$$

$$777 + 20 =$$

$$777 + 200 =$$

$$235 + 3 =$$

$$235 + 30 =$$

$$235 + 300 =$$
  

$$111 + \boxed{\phantom{00}} = 118$$

$$604 + 20 =$$

$$604 + 50 =$$

$$604 + 90 =$$
  

$$111 + \boxed{\phantom{00}} = 118$$

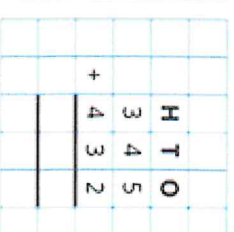
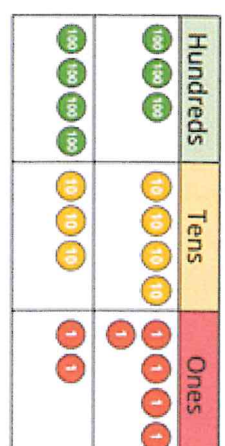
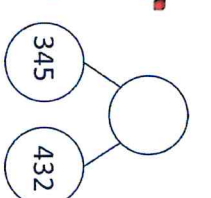
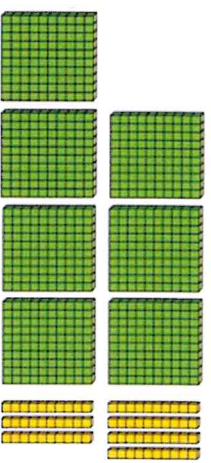
$$111 + \boxed{\phantom{00}} = 181$$

$$111 + \boxed{\phantom{00}} = 811$$

Add two numbers (no exchange)

Mental strategies and introduction of formal written method.

... ones + ... ones = ... ones  
 ... tens + ... tens = ... tens  
 ... hundreds + ... hundreds = ... hundreds



345	?
	432

# Addition

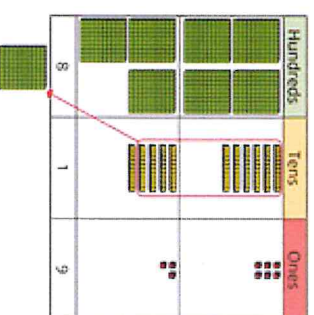
## Progression of skills

Add two numbers across a 10 or 100

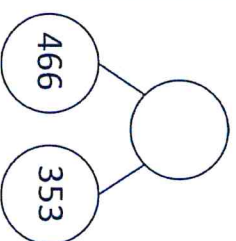
Formal written method involving up to 2 exchanges including 3-digit plus 2-digit numbers.

## Key representations

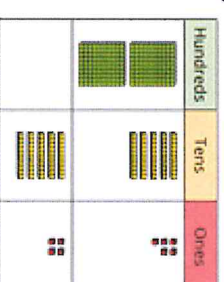
There are ... ones, so I do/do not need to make an exchange.  
There are ... tens, so I do/do not need to make an exchange.  
... ones = ... ten and ... ones.  
... tens = ... hundred and ... tens.



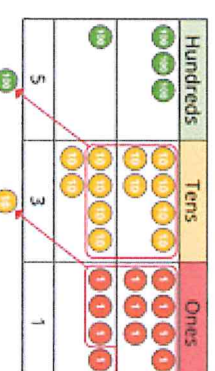
H	T	O
4	6	6
+	3	5
-----		
8	1	9



?	54
-----	
255	



H	T	O
2	5	5
+	5	4
-----		
7	0	9

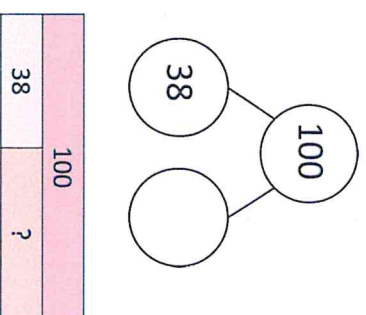
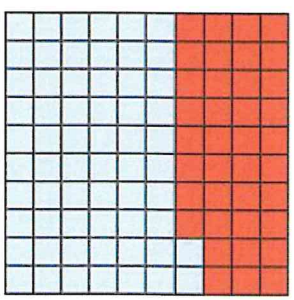


H	T	O
4	6	6
+	3	5
-----		
8	1	9

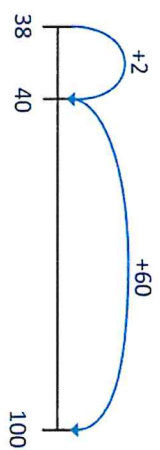
## Complements to 100

Pairs of numbers which total 100

... plus ... is equal to 100



I add ... to get to the next 10, then ... to get to 100



$$38 + 62 = 100$$




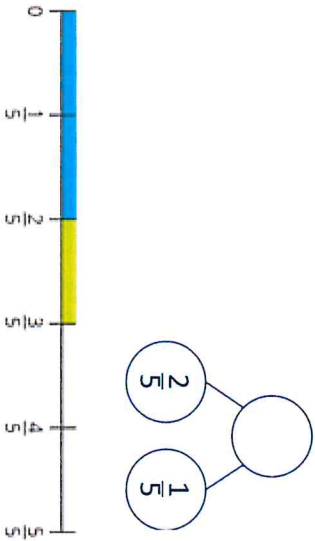

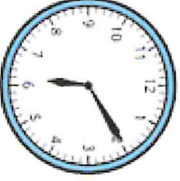
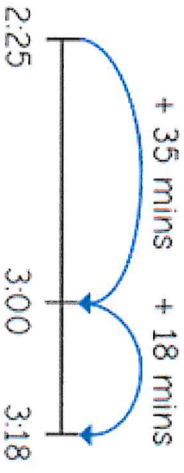
$$62 + 38 = 100$$

$$100 = 38 + 62$$

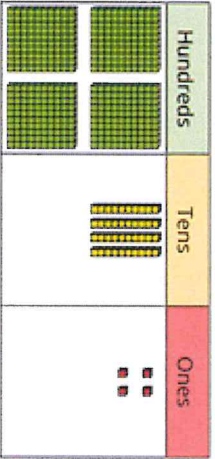
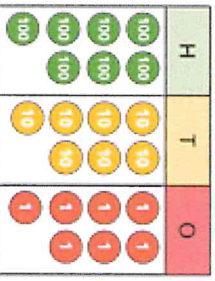
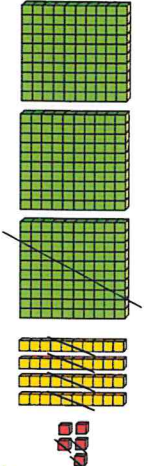
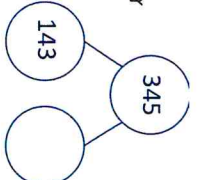
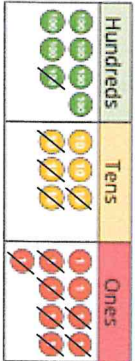
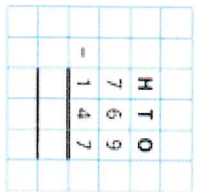
$$100 = 62 + 38$$



# Addition

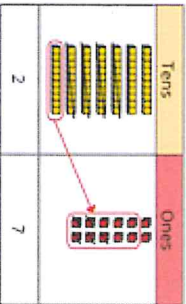
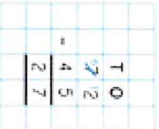
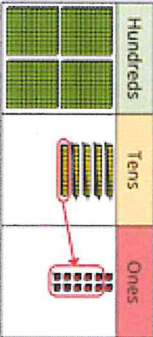

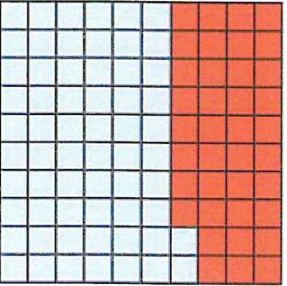

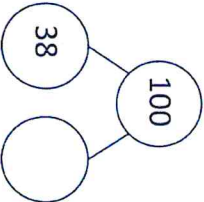
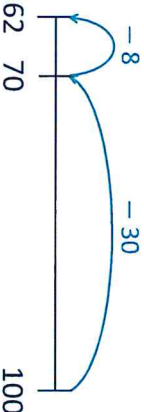
Progression of skills	Key representations
<p><b>Add fractions with the same denominator within 1 whole</b></p> <p>Make links with known facts.</p>	<p>When adding fractions with the same denominator, I only add the numerator. ... fifths + ... fifths = ... fifths</p> <div style="display: flex; justify-content: space-around;"> <div style="text-align: center;">  <math display="block">\frac{1}{5} + \frac{1}{5}</math> </div> <div style="text-align: center;">  <math display="block">\frac{1}{5} + \frac{2}{5}</math> </div> <div style="text-align: center;">  <math display="block">\frac{2}{5} + \frac{3}{5}</math> </div> </div> <div style="text-align: right; margin-top: 20px;">  </div>
<p><b>Calculate the duration of events</b></p> <p>Find durations of time between a given start and end point. Children will need to calculate complements to 60</p>	<p>From ... to ... o'clock is ... minutes. From ... o'clock to ... is ... minutes. The total time taken is ... minutes.</p> <div style="display: flex; justify-content: space-around; align-items: center;"> <div style="text-align: center;">  <p>start</p> </div> <div style="text-align: center;">  <p>finish</p> </div> <div style="text-align: center;"> <div style="border: 1px solid blue; padding: 5px; display: inline-block;">4:25</div> <p>start</p> </div> <div style="text-align: center;"> <div style="border: 1px solid blue; padding: 5px; display: inline-block;">4:55</div> <p>finish</p> </div> </div> <div style="text-align: right; margin-top: 20px;">  </div>

# Subtraction

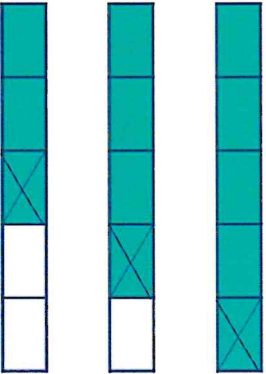
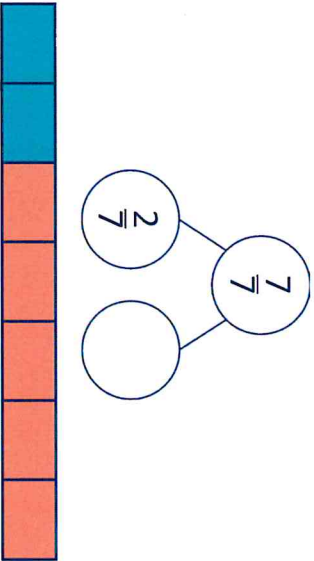
<p><b>Year 3</b></p>	<ul style="list-style-type: none"> <li>Subtract numbers mentally, including: a three-digit number and ones, a three-digit number and tens, a three-digit number and hundreds.</li> <li>Subtract numbers with up to three digits, using formal written methods.</li> <li>Subtract fractions with the same denominator within 1 whole.</li> </ul>	
<p><b>Progression of skills</b></p>	<p><b>Key representations</b></p>	
<p><b>Subtract 1s, 10s and 100s from a 3-digit number</b></p> <p>Emphasis on mental strategies including number bonds and related facts.</p> <p>Prompt children to notice which digit changes.</p>	<p>The ones/tens/hundreds column will decrease by ...</p>  $444 - 2 =$ $444 - 20 =$ $444 - 200 =$ 	<p>What patterns do you notice?</p> $235 - 3 =$ $235 - 30 =$ $235 - 300 =$ $118 - \square = 111$ $181 - \square = 111$ $624 - 20 =$ $654 - 50 =$ $694 - 90 =$ $811 - \square = 111$
<p><b>Subtract two numbers (no exchange)</b></p> <p>Mental strategies and introduction of formal written method.</p>	<p>... ones — ... ones = ... ones</p> <p>... tens — ... tens = ... tens</p> <p>... hundreds — ... hundreds = ... hundreds</p>  	 



# Subtraction

Progression of skills	Key representations											
<p><b>Subtract two numbers across a 10 or 100</b></p> <p>Formal written method involving up to 2 exchanges including 3-digit subtract 2-digit numbers.</p>	<p>I need to subtract ... ones. I do/do not need to make an exchange. I need to subtract ... tens. I do/do not need to make an exchange. I can exchange 1 ... for 10 ...</p>  <table border="1" data-bbox="994 622 1077 907"> <tr><td>72</td><td>?</td></tr> <tr><td>45</td><td>?</td></tr> </table> 	72	?	45	?	<p>I subtract ... tens, then I subtract ... ones.</p>  <table border="1" data-bbox="957 1489 1136 1646"> <tr><td>452</td><td>?</td></tr> <tr><td>178</td><td>?</td></tr> <tr><td>187</td><td>?</td></tr> </table> 	452	?	178	?	187	?
72	?											
45	?											
452	?											
178	?											
187	?											
<p><b>Complements to 100</b></p> <p>Focus on subtraction facts. Encourage children to notice patterns.</p>	<p>100 minus ... is equal to ...</p>   	 <p> <math>100 - 38 = 62</math>  <math>100 - 62 = 38</math>  <math>62 = 100 - 38</math>  <math>38 = 100 - 62</math> </p>										

# Subtraction

Progression of skills	Key representations
<p>Subtract fractions with the same denominator within 1 whole</p> <p>Make links with known facts.</p>	<p>When subtracting fractions with the same denominator, I only subtract the numerator.</p> <p>... fifths — ... fifths = ... fifths</p>  <p><math>\frac{5}{5} - \frac{1}{5}</math></p> <p><math>\frac{4}{5} - \frac{1}{5}</math></p> <p><math>\frac{3}{5} - \frac{1}{5}</math></p> 



# Multiplication

Year 3

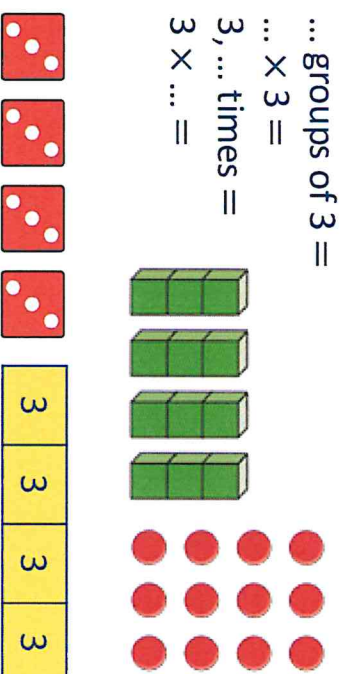
- Recall and use multiplication facts for the 3, 4 and 8 multiplication tables.
- Write and calculate mathematical statements for multiplication using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.
- Solve problems, including missing number problems, involving multiplication, including positive integer scaling problems and correspondence problems in which  $n$  objects are connected to  $m$  objects.

Progression of skills

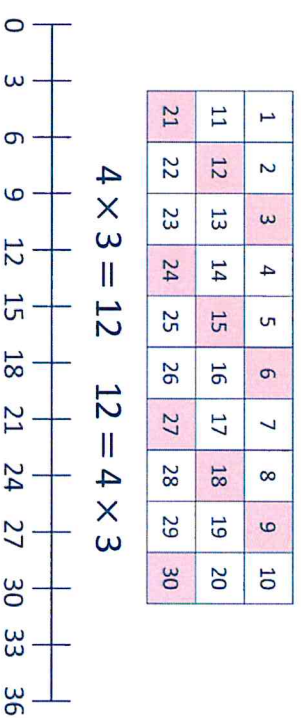
Key representations

The 3 times-table

Encourage daily counting in multiples both forwards and back.

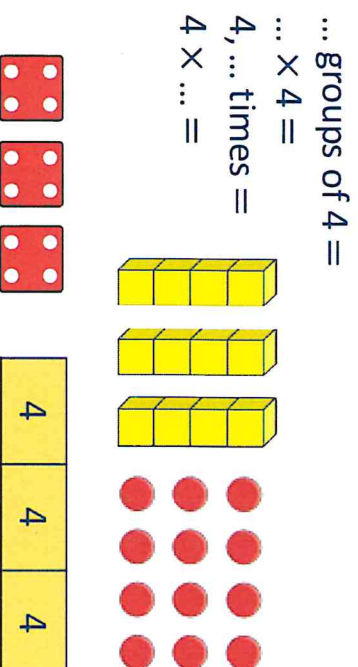


... times 3 is equal to ...

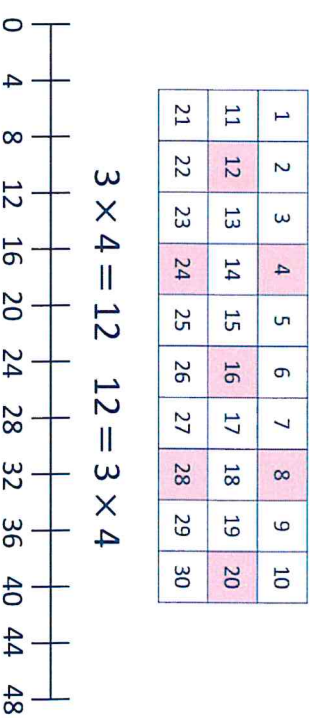


The 4 times-table

Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2 and 4 times-tables.

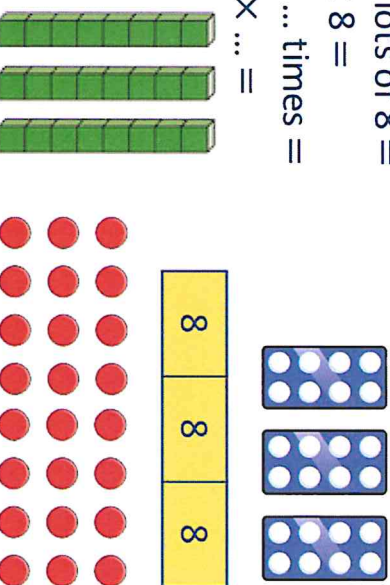
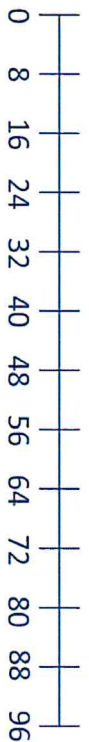
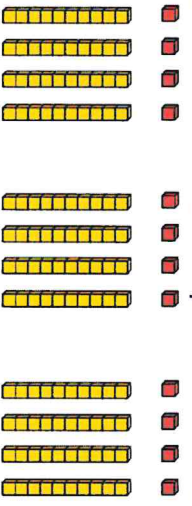
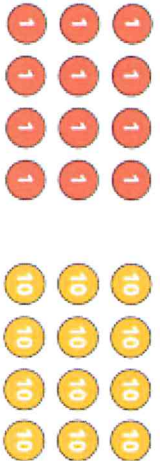
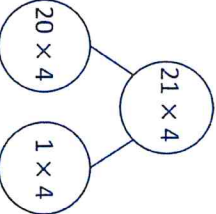


... times 4 is equal to ...





# Multiplication











Progression of skills	Key representations																															
<p><b>The 8 times-table</b></p> <p>Encourage daily counting in multiples both forwards and back. Encourage children to notice links between the 2, 4 and 8 times-tables.</p>	<p>... lots of 8 =  <math>\times 8 =</math>            8, ... times =  <math>8 \times \dots =</math></p> 	<p>... times 8 is equal to ...</p> <table border="1" data-bbox="1037 1411 1197 1971"> <tr><td>1</td><td>2</td><td>3</td><td>4</td><td>5</td><td>6</td><td>7</td><td>8</td><td>9</td><td>10</td></tr> <tr><td>11</td><td>12</td><td>13</td><td>14</td><td>15</td><td>16</td><td>17</td><td>18</td><td>19</td><td>20</td></tr> <tr><td>21</td><td>22</td><td>23</td><td>24</td><td>25</td><td>26</td><td>27</td><td>28</td><td>29</td><td>30</td></tr> </table> <p><math>3 \times 8 = 24</math>    <math>24 = 3 \times 8</math></p> 	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19	20	21	22	23	24	25	26	27	28	29	30
1	2	3	4	5	6	7	8	9	10																							
11	12	13	14	15	16	17	18	19	20																							
21	22	23	24	25	26	27	28	29	30																							
<p><b>Related facts</b></p> <p>Use knowledge of multiplying by 10 to scale times-table facts.</p>	<p>... <math>\times</math> ... ones is equal to ... ones            so ... <math>\times</math> ... tens is equal to ... tens.</p> 	 <p><math>3 \times 4 = 12</math>  <math>3 \times 40 = 120</math></p>																														
<p><b>Multiply a 2-digit number by a 1-digit number - no exchange</b></p> <p>Children apply their understanding of partitioning to represent and solve calculations using the expanded method.</p>	<p>... tens multiplied by ... is equal to ... tens.            ... ones multiplied by ... is equal to ... ones.</p> <table border="1" data-bbox="167 627 406 974"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table> <p><math>30 \times 2 = 60</math>  <math>2 \times 2 = 4</math>  <math>32 \times 2 = 64</math></p>	Tens	Ones					 <table border="1" data-bbox="167 1657 406 2027"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table>	Tens	Ones																						
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# Multiplication

Progression of skills	Key representations																					
<p><b>Multiply a 2-digit number by a 1-digit number - with exchange</b></p> <p>Children apply their understanding of partitioning to represent and solve calculations using the expanded method.</p>	<p>... tens multiplied by ... is equal to ... tens. ... ones multiplied by ... is equal to ... ones.</p> <table border="1" data-bbox="790 638 1141 1019"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table> <p> <math>20 \times 4 = 80</math>  <math>4 \times 4 = 16</math>  <math>24 \times 4 = 96</math> </p>	Tens	Ones									<p>... is ... times the size of ... ... is ... times the length/height of ...</p> <div data-bbox="813 1355 1037 1579"> </div> <table border="1" data-bbox="821 1612 1029 2027"> <thead> <tr> <th>Tens</th> <th>Ones</th> </tr> </thead> <tbody> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> <tr> <td></td> <td></td> </tr> </tbody> </table>	Tens	Ones								
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<p><b>Scaling</b></p> <p>Children focus on multiplication as scaling (... times the size) as opposed to repeated addition.</p>	<p>There are ... times as many ... as ...</p> <div data-bbox="406 638 582 1288"> </div> <p>There are 3 times as many triangles as circles.</p>	<p>... is ... times the size of ... ... is ... times the length/height of ...</p> <div data-bbox="295 1355 614 2060"> </div> <p>Miss Smith is twice the height of Jo.</p>																				

# Multiplication

Progression of skills	Key representations									
<p><b>Correspondence problems</b> (How many ways?)</p> <p>Encourage children to work systematically to find all the different possible combinations.</p>	<p>For every ... , there are ... possible ... There are ... X ... possibilities altogether.</p> 	<table border="1" data-bbox="798 1064 1165 1377"> <thead> <tr> <th>hats</th> <th>scarves</th> </tr> </thead> <tbody> <tr> <td>blue</td> <td></td> </tr> <tr> <td>orange</td> <td></td> </tr> <tr> <td>purple</td> <td></td> </tr> </tbody> </table> <p>For every hat, there are two possible scarves. <math>3 \times 2 = 6</math></p> <p>There are 6 possibilities altogether.</p>	hats	scarves	blue		orange		purple	
hats	scarves									
blue										
orange										
purple										



# Division

**Year 3**

- Recall and use division facts for the 3, 4 and 8 multiplication tables.
- Write and calculate mathematical statements for division using the multiplication tables that they know, including for two-digit numbers times one-digit numbers, using mental and progressing to formal written methods.
- Recognise, find and write fractions of a discrete set of objects: unit fractions and non-unit fractions with small denominators.

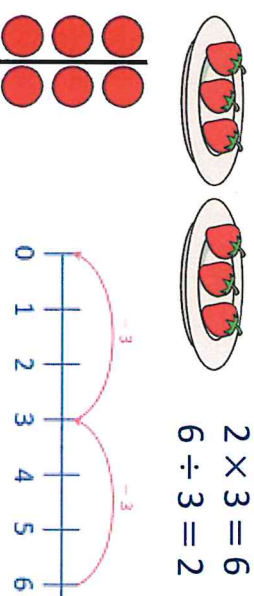
**Progression of skills**

**Key representations**

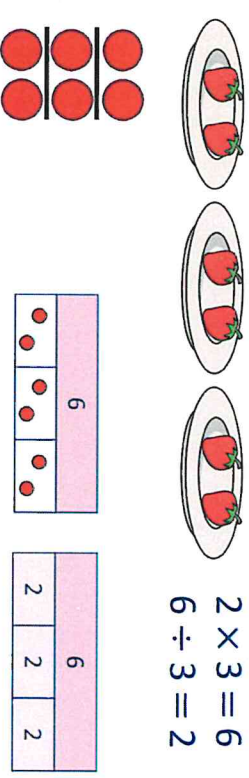
**Divide by 3**

Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.

There are ... groups of 3 in ...  
 $\dots \div 3 =$



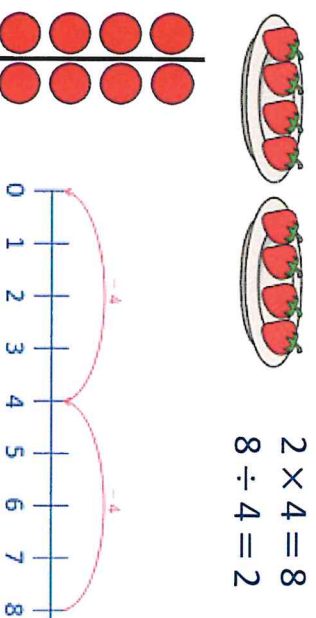
... has been shared equally into 3 equal groups.  
 $\dots \div 3 =$



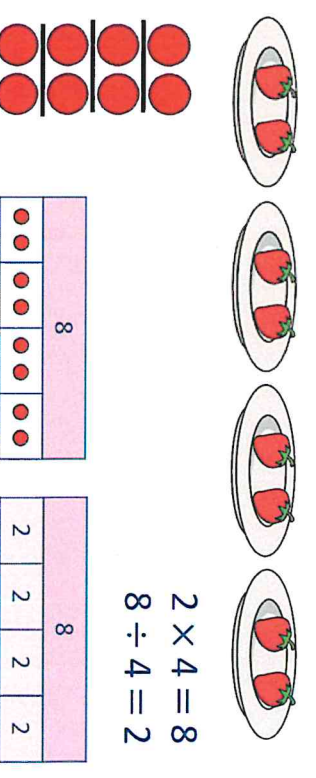
**Divide by 4**

Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.

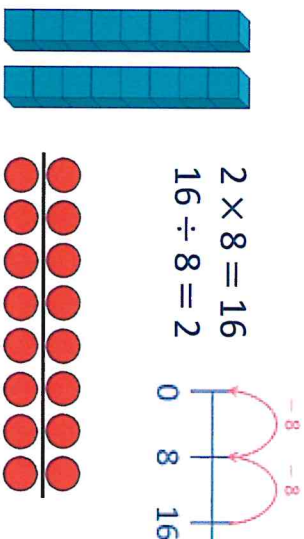
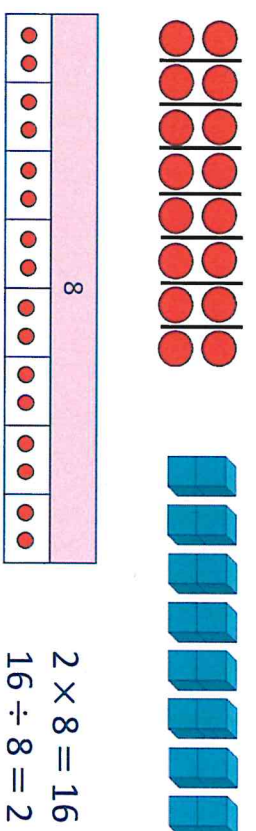
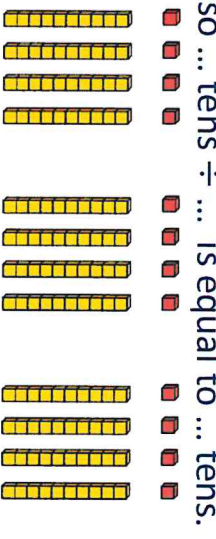
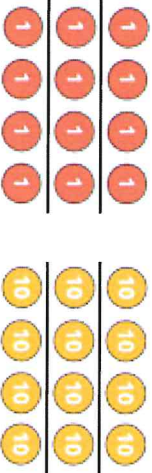
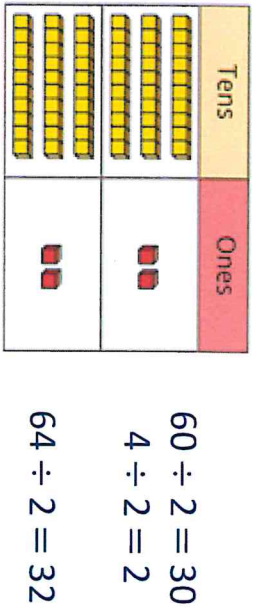
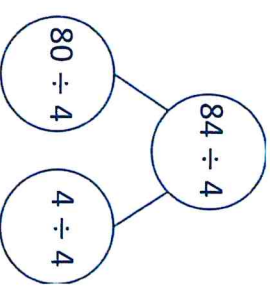
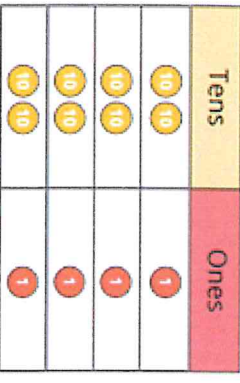
There are ... groups of 4 in ...  
 $\dots \div 4 =$



... has been shared equally into 4 equal groups.  
 $\dots \div 4 =$



# Division

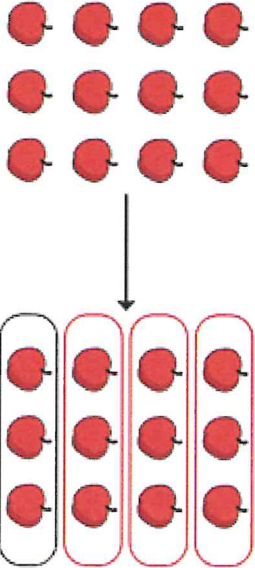
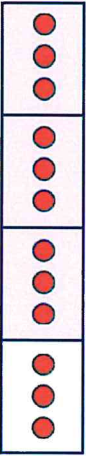
Progression of skills	Key representations
<p><b>Divide by 8</b></p> <p>Encourage children to compare the grouping and sharing structures of division and to make links with times-table facts.</p>	<p>There are ... groups of 8 in ...  <math>\dots \div 8 =</math></p>  <p><math>2 \times 8 = 16</math>  <math>16 \div 8 = 2</math></p> <p>... has been shared equally into 8 equal groups.  <math>\dots \div 8 =</math></p>  <p><math>2 \times 8 = 16</math>  <math>16 \div 8 = 2</math></p>
<p><b>Related facts</b></p> <p>Link to known times-table facts.</p>	<p>... <math>\div</math> ... is equal to ...,          so ... tens <math>\div</math> ... is equal to ... tens.</p>  <p><math>12 \div 3 = 4</math>  <math>120 \div 3 = 40</math></p> 
<p><b>Divide a 2-digit number by a 1-digit number - no exchange</b></p> <p>Partition into tens and ones to divide and then recombine.</p>	<p>... tens divided by ... is equal to ... tens.          ... ones divided by ... is equal to ... ones.</p>  <p><math>60 \div 2 = 30</math>  <math>4 \div 2 = 2</math>  <math>64 \div 2 = 32</math></p>  



# Division

Progression of skills	Key representations	
<p><b>Divide a 2-digit number by a 1-digit number - with remainders</b></p> <p>Encourage children to partition numbers flexibly to help them to divide more efficiently.</p>	<p>... tens divided by ... is equal to ... tens. ... ones divided by ... is equal to ... ones.</p> <p> <math>96 \div 4</math>  <math>80 \div 4</math>  <math>16 \div 4</math>  <math>80 \div 4 = 20</math>  <math>16 \div 4 = 4</math>  <math>96 \div 4 = 24</math> </p>	<p>There are ... groups of ... There are ... remaining.</p> <p><math>31 \div 4 = 7 \text{ r}3</math></p> <p><math>94 \div 4 = 23 \text{ r}2</math></p>
<p><b>Unit fractions of a set of objects</b></p> <p>Bar models are useful to show the link between division and fractions, for example, dividing by 3 and finding a third.</p>	<p>The whole is divided into ... equal parts. Each part is <math>\frac{1}{\square}</math> of the whole.</p> <p><math>\frac{1}{4}</math> of 12 apples is 3 apples.</p>	<p>One ... of ... is ...</p> <p><math>\frac{1}{4}</math> of 12 is 3</p> <p><math>\frac{1}{3}</math> of 36 is 12</p>

# Division

Progression of skills	Key representations	
<p><b>Non-unit fractions of a set of objects</b></p> <p>Bar models are a useful representation and show the links with division and multiplication.</p>	<p>The whole is divided into ... equal parts. Each part is <math>\frac{1}{\square}</math> of the whole.</p>  <p><math>\frac{3}{4}</math> of 12 apples is 9 apples.</p>	<p><math>\frac{1}{\square}</math> of ... is ..., so <math>\frac{\square}{\square}</math> of ... is ...</p> <p><math>\frac{3}{4}</math> of 12 is 9</p>  <p><math>\frac{2}{3}</math> of 36 is 24</p> 